

Online Deep Clustering with Video Track Consistency

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Abstract—Several unsupervised and self-supervised approaches have been developed in recent years to learn visual features from large-scale unlabeled datasets. Their main drawback however is that these methods are hardly able to recognize visual features of the same object if it is simply rotated or the perspective of the camera changes. To overcome this limitation and at the same time exploit a useful source of supervision, we take into account video object tracks. Following the intuition that two patches in a track should have similar visual representations in a learned feature space, we adopt an unsupervised clustering-based approach and constrain such representations to be labeled as the same category since they likely belong to the same object or object part. Experimental results on two downstream tasks on different datasets demonstrate the effectiveness of our Online Deep Clustering with Video Track Consistency (ODCT) approach compared to prior work, which did not leverage temporal information. In addition we show that exploiting an unsupervised class-agnostic, yet noisy, track generator yields to better accuracy compared to relying on costly and precise track annotations.

I. INTRODUCTION

Convolutional Neural Networks (CNNs) are being widely used as the main framework in many computer vision applications due to their great ability to learn different levels of general visual features. Over the past 10 years, their performance has continued to improve, thanks to complex architectures and large-scale datasets. The success of CNNs is, in fact, highly dependent on their capabilities to model highly non-linear patterns and the amount of training data available. The deeper and more expressive the network is, the larger the required dataset will be to effectively train such model.

Models trained on large-scale, fully-supervised and diverse image datasets, such as ImageNet [1] and YFCC100M [2], have been demonstrated to capture common and generic visual features, making them also ideal as a starting point for diverse subsequent learning tasks. According to this view, collecting and annotating in a precise way larger and more diversified datasets to be used in supervised machine learning seems a natural approach to go forward. However, on the other hand, this approach is extremely costly, time consuming and requires a massive amount of manual annotations. As a consequence, unsupervised learning has recently received attention in the field of machine learning and methods for clustering, dimensionality reduction, and density estimation are commonly used in computer vision applications [3], [4], [5], [6].

The goal of unsupervised representation learning is indeed to learn transferable image or video representations without the need for manual annotations [7], [8], [9], [10], [11], [12], [13]. Clustering-based representation learning approaches, which

jointly optimize clustering and feature learning, stand out as a potential trend in this field [14], [15], [16], [17], [18], [19].

In this work we focus the attention on two unsupervised clustering-based learning methods, DeepCluster (DC) [17] proposed by Caron *et al.* and Online Deep Clustering (ODC) [19] proposed by Zhan *et al.*. Both these methods alternate between deep feature clustering and CNN parameters update, with the difference that ODC proposed to decompose the clustering procedure into mini-batch-wise label updates and incorporate these updates into network update iterations.

Despite the success of such clustering-based methods, they are mostly focused on still images and do not exploit additional sources of supervision such as temporal consistency in videos. Following this idea, we propose a novel unsupervised approach to exploit temporal information from videos, allowing the network to use tracks proposals as a form of self-supervision. Our method, dubbed Online Deep Clustering with Video Track Consistency (ODCT), is fully unsupervised and can be trained starting from any video database, without any prior knowledge regarding the nature of their content. To this end we leverage an unsupervised object discovery approach that extracts class-agnostic track proposals and exploit such data to constrain a feature clustering phase and generate temporal coherent pseudo-labels.

The main contributions of our work are the following:

- We present a fully unsupervised, class-agnostic method exploiting video temporal consistency of object tracks using feature clustering to generate pseudo-labels.
- We show how adding constrains on the clustering phase we can account for intra-track variability and obtain a more effective supervision signal.
- We test our model on two downstream tasks on different datasets, obtaining significant improvements compared to prior work which leverages only still images.

II. RELATED WORK

Unsupervised and Self-Supervised learning are used in representation learning methods to generate feature representations merely from images, without the need for time-consuming semantic annotations. Self-Supervised methods, in particular, employ pre-designed pretext tasks and need no labeled data in order to train the weights of a convolutional neural network. Instead, the visual features are learned by minimizing the pretext task's objective function.

Several pretext tasks have been proposed in the literature and each of them was carefully designed to use various cues

all the features belonging to samples x_j in the same track $F_m(x_j)$. Let x' be the sample in the track with the closest feature vector $F_m(x')$ to $f_\theta(x_i)$. We define weight coefficients d_j , that will be used to update the Samples Memory, as $d_j = \frac{d(x_i, x')}{d(x_i, x_j)}, \forall x_j \in T$

(iv) *Samples Memory Update*: each sample in the current batch is used to update the Samples Memory exploiting the weight coefficients d_j :

$$F_m \leftarrow m \frac{f_\theta(x)}{\|f_\theta(x)\|_2} + (1 - m) \frac{\sum_j d_j F_m(x_j)}{\sum_j d_j} \quad (1)$$

where $m \in (0, 1]$ is a momentum coefficient. At the same time, each sample's pseudo-label is updated by finding its nearest centroid:

$$\arg \min_{p \in \{1..C\}} \|F_m - C_p\|_2^2, \quad (2)$$

where C_p indicates the centroid feature of class p in the Centroids Memory.

(v) *Centroids Memory Update*: every k -th iteration the centroids are updated as the mean of the feature vectors assigned to each cluster.

As in [19], to avoid trivial solutions where all samples are assigned to a single clusters, we prevent small clusters to become empty. Let C_s be the set of clusters with size less than a certain threshold. For $c \in C_s$, we start by assigning samples in c to the nearest centroids belonging to the remaining clusters $C_n = C \setminus C_s$, thus making c empty. Then, the largest cluster $c_{max} \in C_n$ is partitioned into two sub-clusters using *K-Means*. This process is repeated until the set of small clusters C_s is empty.

IV. TRACK GENERATION

To train our model, we assumed to have access to a set of video tracks. For the purpose of our work, these can be provided by some source of track oracle yielding linked bounding boxes in video frames. In the following Sec. V we will discuss experiments performed using ground truth tracks. Nonetheless, since we operate under an unsupervised data-regime, we also rely on an object discovery pipeline, derived from [29], capable of producing a set of class-agnostic tracks which can be exploited to train our model. The idea of such approach is to track spatio-temporal consistency in frame-wise object proposals. We use EdgeBoxes [30] to generate proposal boxes for each frame. These boxes are likely to enclose an object based on low level image characteristics, such as edges, which provide an *objectness* score for regions of interest. Note that this method does not require any class-specific training, thus can be applied to discover any kind of object or part of it. As in [29], we then use a greedy box-association tracker to link proposals across frames based on their spatial consistency through time. To reduce mismatches, we register each frame onto the next by shifting boxes using optical flow. More formally, we can define a track as a succession of bounding boxes b_i^k , for which the intersection over union (IoU) between two boxes of consecutive frames, b_i^n, b_{i+1}^m , is

greater than a threshold θ_τ . We can define as well the track score S_{t_j} for track t_j , as the mean objectness score of its boxes $S_{t_j} = \frac{\sum_{i \in t_j} s_i^k}{|t_j|}$ where $|t_j|$ indicates the total number of boxes in track t_j . This naturally leads to a track ordering.

An issue with matching bounding boxes is that there might be missing frames and therefore track fragmentation due to occlusion or appearance changes. As in [30] we use a Time to Live counter (TTL), which represents the maximum number of frames without match before truncating a track. Finally, we apply a post-processing step to remove the tracks that are unlikely to represent objects. Particularly, we consider only tracks with a length between l and L , as we believe that shorter, more consistent tracks are preferable to longer tracks that are likely to be subject to errors, due to static background, noise, object occlusion or camera movement. l and L are empirically set to 40 and 100, respectively. In order to retain only tracks that are likely to represent objects, we retain only the first 15 tracks in each snippet.

V. EXPERIMENTS

In this Section, we present experimental results. In addition to our *ODC with Video Track Consistency* (ODCT) model, for the purpose of evaluation we report results from two additional methods. The first is vanilla ODC [19], trained on the same video data as ODCT. This does not integrate temporal knowledge from video snippets in any way and relies purely on clustering visually similar items. Then we propose a simple ODC variant with our modified *K-Means* procedure used for initialization, which constrains crops belonging to the same track to be assigned to the same cluster. We will refer to this model as $ODC_{TrackInit}$.

We apply a two-step training procedure, commonly adopted for unsupervised learning [17], [19]: (i) First, we perform unsupervised pre-training using the unsupervised pretext methods on a pre-training dataset. Usually, such dataset is large yet with limited or no annotation. (ii) We then perform transfer learning by fine-tuning the model on some downstream task, i.e. harder tasks with access to some form of supervision.

A. Datasets and Data Preprocessing

We conduct our pre-training experiments on the ImageNet VID 2015 dataset [31], a dataset designed for object tracking and object detection. It includes videos of 30 basic object categories, subset of the 1,000 ILSVRC-2012[1] classes. In total, ImageNet VID consists of 3,862 snippets for training, 555 snippets for validation, and 937 snippets for testing. All snippets include 56 to 458 frames of images, with a median frame rate and duration of 29fps and 12s, respectively. Each frame is annotated with labels indicating the presence of the 30 object classes and their corresponding bounding boxes. The dataset comprises a total of 7,857 ground truth tracks for training. In our experiments we will initially discard such annotations in order to work in a fully unsupervised regime, but we will also train our model using ground truth tracks as a control experiment in Sec. V-F. As downstream tasks we follow commonly adopted benchmarks as in [9], [17], [19]

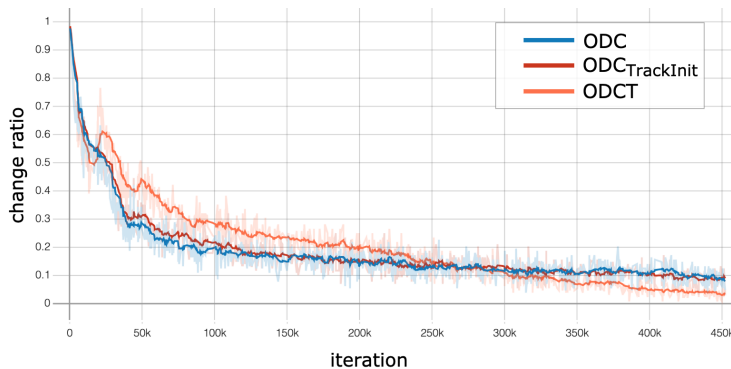


Fig. 2. Change ratio for sample-cluster assignments during training.

and evaluate our model on ImageNet [1] and Pascal VOC 2007 [32].

We scale all frames to the same maximum dimension of 600px. As described in Sec. IV, we perform the object proposal phase with EdgeBoxes. To reduce noise, we limit the number of proposals per frame to 300, before applying non-maximal suppression (NMS) to select the best bounding box for each object. In the box tracking phase, we set the Time To Live counter (TTL) to 3 frames and the IoU threshold for bounding box matching to 0.35. Furthermore, we removed bounding boxes with an area smaller than 10,000 square pixels. We collected 57,879 tracks, each of which has been subsampled by picking 10 frames, equally spaced in time, for a total of 578,790 training samples. Object crops are resized to a resolution of 224x224 and data augmentation is applied including random flipping, rotation ($\pm 2^\circ$) and color jittering. In addition, we randomly convert images to grayscale with a probability of 0.2. Applying random color jitter and grayscale transformations on the training samples, discourages the network from exploiting trivial information from color to group samples snippet-wise.

B. Training Details

We employ ResNet-50 as model backbone and introduce a non-linear head to reduce hidden size dimensionality for storing features in the external memories. The head is composed of a 512-dimensional fully connected layer, followed by batch normalization, another 256-dimensional fully connected layer with relu activation and dropout. The head layer is removed for downstream tasks.

All the models are trained from scratch on a single GeForce RTX 2080 Ti GPU with mixed precision training for efficiency. The batch size and the learning rate are respectively set to 128 and 0.015 for 100 epochs using the SGD optimizer with momentum set to 0.5. The threshold to identify small clusters is set, as in ODC, to 20. Zhan *et al.* [19] proved that changing this threshold does not affect the results significantly, as long as it does not exceed the average number of samples in a cluster. Regarding the Centroids Memory update, we

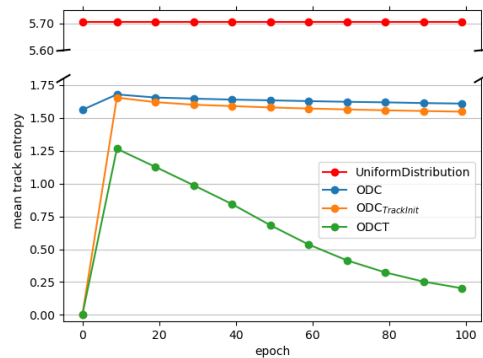


Fig. 3. Mean track entropy for cluster assignments during training. We also report the entropy for a Uniform Distribution over clusters as an upper bound.

perform it every 10 iterations to balance learning efficacy and efficiency. Following Caron *et al.* [17], we use a number of clusters equal to 10 times the number of annotated categories in the dataset ($K=300$). However, as an ablation study, we also trained our model using $K=30$ and $K=1000$.

C. Preliminary evaluation

In a preliminary set of experiments, we analyze the models' behavior during training.

1) *Cluster reassignments*: To assess the models' stability, we keep track of the change ratio, i.e. the fraction of samples whose labels change at each iteration. Intuitively, fewer label switches indicate better stability. In Fig. 2 we illustrate the change ratio during training for ODC, $ODC_{TrackInit}$ and ODCT, trained from scratch, with $K = 300$ clusters. Models with $K = 30, 1000$ presented similar trends. Initially, almost 100% of samples undergo a label switch. The ratio decreases gradually and converges to ~ 0.1 , thus indicating stability for 9 samples out of 10. Interestingly, $ODC_{TrackInit}$ and ODC have almost identical curves, while ODCT initially exhibits a higher change ratio but is able to eventually converge to a more stable solution (~ 0.04).

2) *Cluster entropy*: To assess how well the models assigns samples from the same track to the same cluster, we rely on an entropy based evaluation. Given a cluster assignment, for each track T we can determine the sample distribution over the K clusters, counting the occurrences of track samples per each cluster, $X_T = \{x_1, x_2, \dots, x_K\}$. We then compute the Shannon entropy H , for X_T , as $H(X_T) = -\sum_{i=1}^K x_i \log(x_i)$. This measures how noisy the distribution of track samples is over clusters. Ideally, samples of a same track should belong to the same cluster, yielding entropy $H(X_T) = 0$.

In Fig. 3 we report the mean track entropy computed for all the ImageNet VID track proposals during training. At the first epoch, we have $H(X_T) = 0$ for $ODC_{TrackInit}$ and ODCT since all the samples in a track are associated to the same cluster and same pseudo-label. $ODC_{TrackInit}$ mostly follows the same trend as ODC, meaning that initialization alone does not suffice to obtain an effective clustering during training.

TABLE I

TOP-1 CLASSIFICATION ACCURACY ON IMAGENET (LEFT) AND MAP ON PASCAL VOC 2007 (LEFT). ODC*[19]: ODC PRE-TRAINED ON IMAGENET. *ImageNet labels*: FULLY SUPERVISED RESNET-50 PRE-TRAINING ON IMAGENET. *Random*: RESNET-50 WITH RANDOM WEIGHTS. ALL OTHER MODELS ARE PRE-TRAINED ON IMAGENET VID WITHOUT SUPERVISION.

ImageNet	Method	Stage1	Stage2	Stage3	Stage4	Stage5	VOC07	Method	Stage1	Stage2	Stage3	Stage4	Stage5
	ImageNet labels[19]	15.18	33.96	47.86	67.56	76.17		ImageNet labels[19]	26.84	47.56	58.94	78.94	87.17
	Random[19]	11.37	16.21	13.47	9.07	6.54		Random[33]	9.60	8.30	8.10	8.00	7.70
	ODC*[19]	14.76	31.82	42.44	55.76	57.70		ODC*[19]	27.33	46.16	56.22	68.06	78.42
$K = 30$	ODC	10.63	21.74	23.01	22.86	16.65	$K = 30$	ODC	24.80	39.36	40.02	36.72	30.85
	ODC _{TrackInit}	10.61	22.27	24.10	24.07	17.34		ODC _{TrackInit}	24.86	38.76	40.00	37.88	31.32
	ODCT	10.91	23.50	27.37	30.26	23.38		ODCT	24.58	39.74	42.80	43.83	38.28
$K = 300$	ODC	9.95	21.92	23.70	23.35	16.74	$K = 300$	ODC	24.01	38.67	39.57	37.55	31.62
	ODC _{TrackInit}	10.39	21.74	25.56	25.86	19.20		ODC _{TrackInit}	24.87	38.85	41.47	38.70	33.10
	ODCT	11.02	24.54	28.06	32.23	26.00		ODCT	24.77	41.00	44.56	45.55	41.38
$K = 1000$	ODC	11.14	21.25	23.65	23.14	16.80	$K = 1000$	ODC	24.22	38.36	39.56	37.57	31.58
	ODC _{TrackInit}	11.39	23.11	24.82	25.93	19.53		ODC _{TrackInit}	24.74	39.63	40.50	38.77	33.37
	ODCT	11.44	24.79	28.72	32.95	26.04		ODCT	25.08	41.28	44.57	46.23	41.74

Nonetheless, it still obtains a slightly lower entropy value than vanilla ODC, indicating that a good initialization indeed has a beneficial effect. ODCT, on the other hand, due to the constrained Samples Memory update, exhibits a completely different trend, managing to effectively lower the mean track entropy epoch by epoch.

D. Transfer Learning Experiments

As in [34], we extract image features from our ResNet-50 pretrained on Imagenet VID, truncating the model after the last layer of every residual stage in ResNet-50. In the following we discuss the downstream tasks we adopted to evaluate our pre-trained model and the quality of such features.

1) *ImageNet Linear Classification*: As proposed by Zhang *et al.* in [9], we test the task generalization of the representation by freezing the backbone’s weights and training linear classifiers on top of each layer to perform 1000-way ImageNet classification. We report top-1 center-crop accuracy on the validation split of ImageNet. Results are shown in Tab. I (left). We compare our model against ResNet-50 trained directly on ImageNet in a fully supervised setting and against a version with random weights, as proposed in [35]. Such methods act as an upper bound and lower bound for the task, respectively. We also report results for ODC pretrained on ImageNet, as reference. We compare our model to ODC pretrained on ImageNet VID for different number of clusters values. All models are trained for 100 epochs, using SGD with momentum of 0.9 and batch size of 64. The learning rate is initialized as 0.01 and decayed by a factor of 10 after every 30 epochs.

We can observe that ODCT Stage1 results in slightly higher accuracy than ODC and ODC_{TrackInit}, with the best improvement using $K = 300$. However, this small performance gap is immediately widened at Stage2, and our ODCT network achieves much higher results compared to standard ODC and ODC_{TrackInit} pre-trained on ImageNet VID. As we use features extracted from deeper layers of the network, we can observe a consistent increase up to Stage4 for all methods. In particular, ODCT exhibits an improvement across all layers, with the best gain ($\sim 33\%$ - 40%) obtained with Stage4 and Stage5 and $K = 300, 1000$. These results indicate that exploiting video track information encourages representations

that linearly separate semantic classes in the trained data distribution.

However, there is no significant improvement using $K = 1000$ compared to $K = 300$. This suggests that, after a certain value of K , the accuracy saturates. Interestingly, we can see that also for ODC_{TrackInit} there is a considerable performance gain compared to vanilla ODC, proving that a good initialization can have a significant impact on the whole training process.

2) *VOC2007 SVM Classification*: We test our model on the classification benchmark PASCAL VOC2007[32]. Following the setup of Goyal *et al.* [33], we train linear SVMs on features extracted from the ResNet-50 backbone on the `trainval` split of VOC07. We follow the same configuration of [33] and report mean Average Precision (mAP) on the test set. The results in Tab. I (right), show that ODCT surpasses ODC, when both are pre-trained on ImageNet VID, by a significant margin on the VOC2007 SVM classification task.

We can observe that, ODCT yields comparable results to ODC_{TrackInit} for $K = 30, 300$ for Stage1. However, starting from Stage2, ODCT achieves higher results throughout the remainder of the network compared to other unsupervised methods pretrained on ImageNet VID. Significantly, with $K = 1000$, ODCT achieves 46.23% mAP with Stage4, which is 6.67% higher than the best performing layer of ODC and 5.73% higher than the best performing layer of ODC_{TrackInit}. Also, our method gains over 10% mAP points with $K = 300, 1000$ compared to ODC on the last layer.

E. Qualitative Analysis

In Fig. 4 we show portions of the clusters obtained training ODCT using $K = 1000$. The number of clusters is much larger than that of the annotated classes and interestingly there are some clusters that represent new semantic categories beyond the annotated ones. In addition to the clusters that represent existing classes in ImageNet VID, shown in the orange box, we find additional subclasses (blue box), e.g. "white car", "car on racing track" or "dog with white snoug".

ODCT also groups images with similar relations between objects. As shown in the yellow box, the method discovers clusters representing "animal on a lawn" and "busses and trains", which have a similar visual appearance. Moreover, due

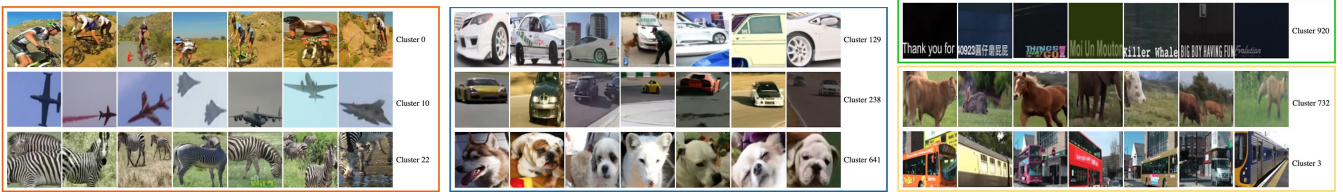


Fig. 4. Samples assigned to different clusters. Orange: existing classes. Blue: subclasses. Green: new classes. Yellow: object relations.

TABLE II
INTRA-TRACK AND INTRA-CLASS ENTROPY COMPUTED WITH GT TRACKS FROM IMAGENET VID. THE LOWER THE BETTER.

	Method	Intra-Track H	Intra-Class H
$K = 30$	ODC _{GT}	0.868	2.986
	ODC _{GT-TrackInit}	0.873	3.013
	ODCT _{GT}	0.061	2.813
$K = 300$	ODC _{GT}	1.368	4.963
	ODC _{GT-TrackInit}	1.360	4.969
	ODCT _{GT}	0.064	4.099

to the unsupervised pre-training on videos, ODCT is capable to detect new classes such as "text on a dark background" (green box in Fig. 4).

F. Training with Ground Truth Tracks

Previous experiments demonstrated that ODCT is effective and achieves a significant improvement in transfer learning tasks when compared to vanilla ODC. Such results are obtained relying on a set of tracks generated without supervision, as outlined in Sec. IV. Since ImageNet VID also contains manually annotated tracks, we retrain our model using GT tracks (discarding class information) to highlight the difference between the two approaches. Our unsupervised track generation method yields a total of 57,879 tracks compared to the 7,857 ground truth tracks annotated in the dataset. Our tracks however, despite being an order or magnitude more, are likely to contain noise, be fragmented or focus on object parts or groups of objects. On the other hand, GT tracks are precise, clean and represent single objects in their entirety.

Following the same setting described in section V-B we train from scratch the three models on the GT ImageNet VID tracks¹, with $K = 30, 300$, discarding class labels. We refer to these models as ODC_{GT}, ODC_{GT-TrackInit} and ODCT_{GT}.

We evaluate the models using two entropy measures:

(i) *Intra-Track Entropy* is used to evaluate the distribution of tracks over clusters. For each track T , we measure how a track is distributed over K clusters by computing the Shannon entropy as in Sec. V-C2, counting the occurrences of track samples per each cluster.

(ii) *Intra-Class Entropy* is a measure of how well a model assigns samples from the same class to the same cluster. For each class, we compute the class distribution over K clusters, counting the occurrences of class samples per each cluster, and then compute the Shannon entropy.

¹We use 10% of equally spaced samples per track, a total of 77,714 samples.

TABLE III
IMAGENET TOP-1 ACCURACY AND PASCAL VOC07 MAP FOR ODCT TRAINED ON UNSUPERVISED TRACKS AND GT TRACKS.

	Method	ImageNet top-1 acc	VOC07 mAP
$K = 30$	ODC	22.86	36.72
	ODC _{TrackInit}	24.07	37.88
	ODCT	30.26	43.83
$K = 30$	ODC _{GT}	19.75	33.77
	ODC _{GT-TrackInit}	20.01	33.36
	ODCT _{GT}	22.49	36.14
$K = 300$	ODC	23.35	37.55
	ODC _{TrackInit}	25.86	38.70
	ODCT	32.23	45.55
$K = 300$	ODC _{GT}	21.33	35.25
	ODC _{GT-TrackInit}	21.42	35.59
	ODCT _{GT}	24.18	37.29

In Tab. II we report the Intra-Track and Intra-Class entropies computed on all tracks. In both the experiments, the entropy for ODCT is lower, thus indicating that our approach assigns samples from the same tracks and classes to the same clusters better than the others. In particular, it is interesting to notice the significant drop in Intra-Track entropy compared to the other methods. This underlines the effectiveness of our clustering strategy, which manages to keep together samples belonging to the same track.

We additionally evaluate the effectiveness of the model trained on the GT tracks using the ImageNet and VOC07 downstream classification tasks. We use the same settings indicated in Sec. V-D1 and Sec. V-D2, considering only Stage4. Results are shown in Tab. III. Interestingly, there is not much difference among all methods using the ground truth annotations, with a gap of at most 2-3 points in either accuracy and mAP. At the same time, it is surprising to notice that unsupervised tracks yield much higher results when comparing models to their counterparts trained with GT tracks. This hints to the fact that, even if manually annotated tracks are clean and precise, it is better to train with more, possibly noisy, data. In addition, our unsupervised track generation can provide tracks from unseen classes that can help to perform a better pre-training.

VI. CONCLUSIONS

In this paper we have introduced an unsupervised clustering-based approach that exploits temporal consistency of video tracks to model intra-class variation. It emerges that simple track based initialization has beneficial effects and overall exploiting temporal information leads to important gains in accuracy compared to prior work based on still images.

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